

# Quiz 8

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**This quiz does not count towards your grade.** It exists to simply gauge your understanding. Treat this as though it were a portion of your midterm or final exam.

## 1 Polynomials

1. **True or False** We can construct two equal polynomials, where one has  $k$  non-zero coefficients  $b_i$  and the other has  $k$  distinct roots  $e_i$  (i.e.,  $\prod_i (x - e_i) = b_{k-1}x^{k-1} \cdots b_1x + b_0$ )
2. **True or False** For some prime  $p$ , we know a polynomial of degree  $p + 1$  is not unique by Fermat's Little Theorem in  $GF(p)$ . Is a polynomial of degree  $p$  unique in  $GF(p)$ ?  $p - 1$ ? (Remember that, for this course,  $GF(p)$  just means all polynomials are taken  $p$ ).
3. From a group, at least  $b$  members must come together to unlock the secret. All members carry the same amount of unique information and  $b - 1$  members are not sufficient. If only  $b - a$  members come together, how many possible polynomials would they need to try? How many possible secrets? Assume this is in  $GF(p)$  for some prime  $p$ . (Consider the case where  $a = 0$ , then  $a = b$ )